

# Runtime Verification of Hyperproperties for Deterministic Programs

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# General Data Protection Regulation\* (GDPR)



“Personal data must be: **adequate, relevant,** and limited to **the minimum necessary** in relation to the **purposes** for which they are processed...”

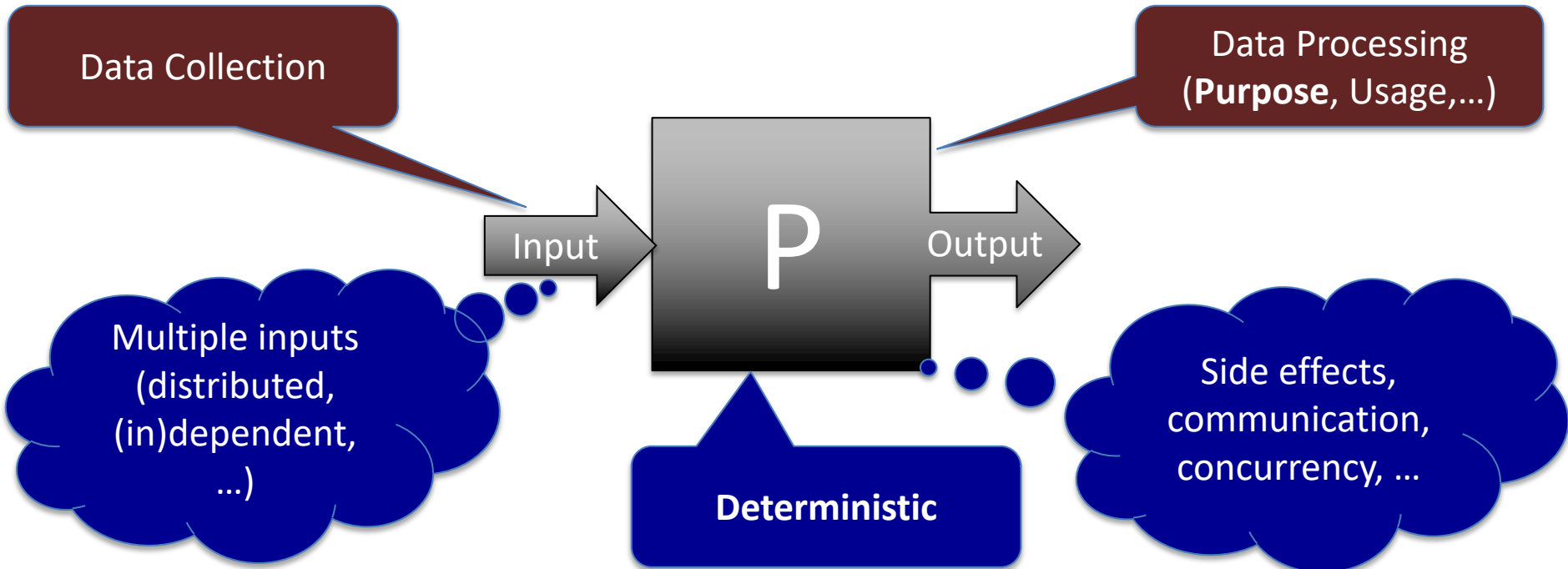
Simplifying: “You should not **collect** more data than what is strictly required for the **intended computation**”

- What might this mean? How can it be ensured?
  - Statically? At runtime?

# What is the connection with the title of our paper?

- The above "principle" is called *Data Minimization*
- Data minimization is a representative of an interesting class of properties
- *Hyperproperties* are properties defined over *sets of sets* of traces
  - "Normal" properties are defined over *sets* of traces

# Data Minimization



Collection vs Usage: We focus on the first (restricted)

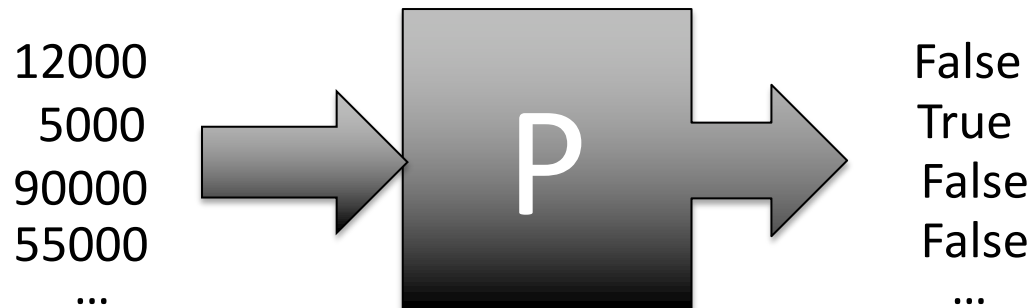
- **Previous work:** Definitions + what can be done statically
  - T. Antignac, D. Sands, and G. Schneider. *Data Minimisation: A Language-Based Approach*. In SEC'17, vol 502 of IFIP AICT, pp. 442-456, 2017
- **Goal of this work:** Monitoring data minimization and other similar hyperproperties

# A Simple Program...

---

```
1 input ( salary );  
2 benefits := ( salary < 10000 );  
3 output ( benefits );
```

---



Is the information about the salary really needed?

# Data Minimization (Minimality)

## Definition

P is **data minimal** if its output is *totally dependent* on its inputs: **any** variation of input  $x$  causes variation in output  $y$

Two variants:

**Monolithic**: a single input source

**Distributed**: multiple independent sources

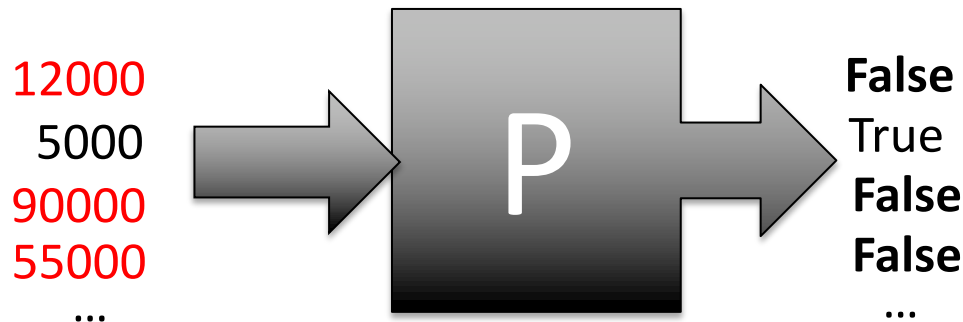
Monolithic case: minimality is just *injectivity*

# Data Minimization (Minimality)

## Definition

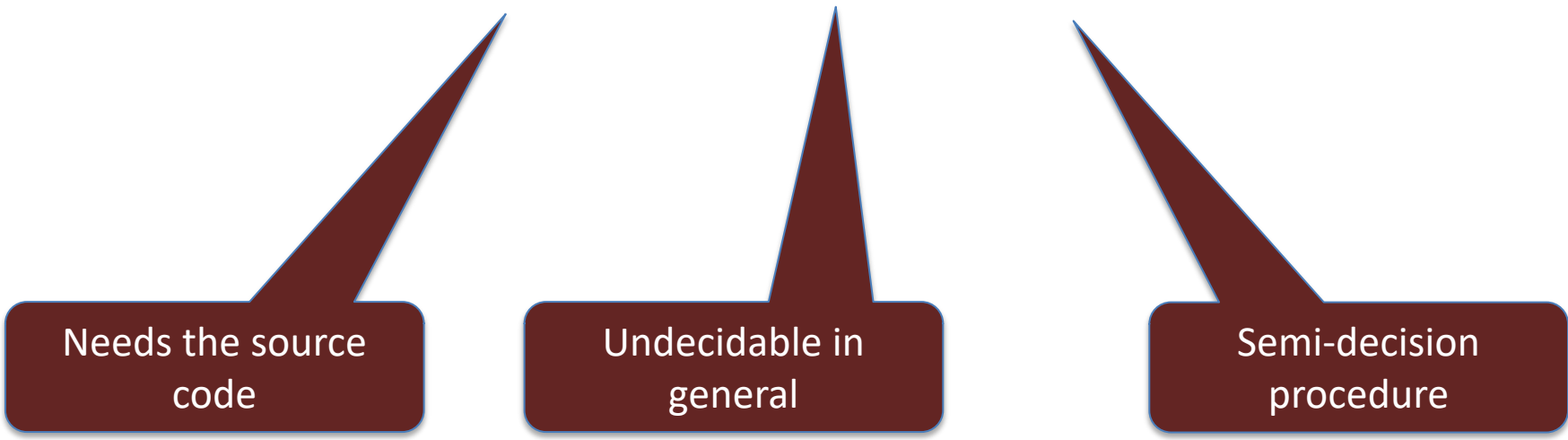
P is **data minimal** if its output is ***totally dependent*** on its inputs: **any** variation of input  $x$  causes variation in output  $y$

P (the “benefits” program) is not (monolithical) minimal



# Why Monitoring?

Statically detecting and ensuring (monolithic and distributed) data minimality is not easy\*



Needs the source  
code

Undecidable in  
general

Semi-decision  
procedure

\* T. Antignac, D. Sands, and G. Schneider. *Data Minimisation: A Language-Based Approach*. In SEC'17, vol 502 of IFIP AICT, pp. 442-456, 2017





# Can we do it?



- M.R. Clarkson, B. Finkbeiner, M. Koleini, K.K. Micinski, M.N. Rabe, C. Sánchez: *Temporal Logics for Hyperproperties*. POST'14
- B. Bonakdarpour and B. Finkbeiner. 2016. *Runtime Verification for HyperLTL*. In RV'16.
- S. Agrawal and B. Bonakdarpour. 2016. *Runtime Verification of  $k$ -Safety Hyperproperties in HyperLTL*. In CSF'16.
- N. Brett, U. Siddique, and B. Bonakdarpour. 2017. *Rewriting-Based Runtime Verification for Alternation-Free HyperLTL*. In TACAS'17.

Monitoring algorithms for the **alternation-free** fragment of  
**HyperLTL**

Universal quantifiers: usually **not** monitorable

Existential quantifiers: monitorable

# What Does it Means for Us?



Data minimization may be expressed in HyperLTL!



We are done then! Somebody else did it!



Yes, but... Algorithms are general for HyperLTL

# (Monolithic) Data Minimization

## Revisited...

Quantification  
over traces

$$\forall \pi, \forall \pi' : \pi_I \neq \pi'_I \implies \pi_O \neq \pi'_O.$$

HyperLTL<sub>2s</sub>

$$\begin{aligned} & \exists \forall \pi, \forall \pi' : \psi \\ \psi ::= & a_\pi \mid \neg \psi \mid \psi \vee \psi \end{aligned}$$

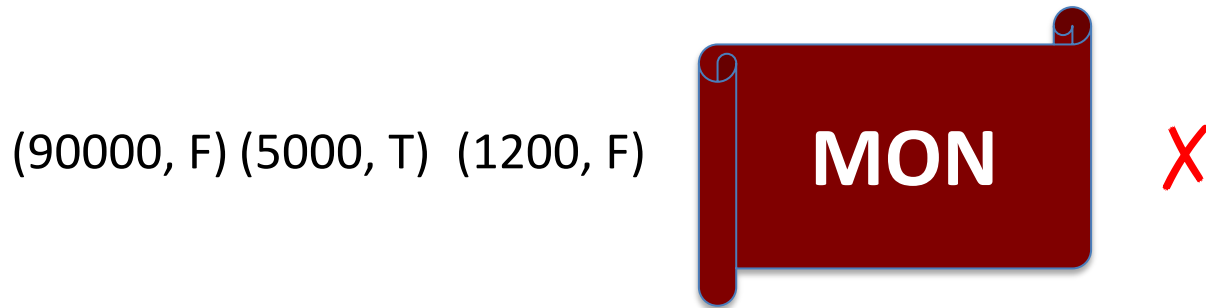
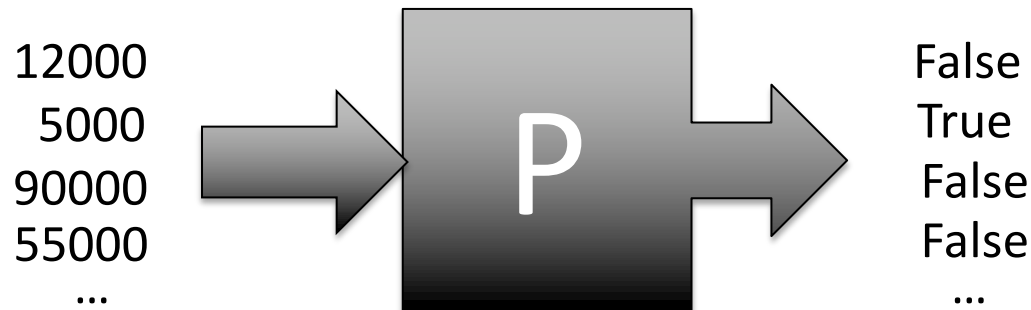
- ***Non-minimality*** is monitorable but it is in general impossible to give a final verdict for minimality!
- Traces are of fixed length (one)
- We are considering deterministic programs
- The property only talks about inputs and outputs!

It should be simpler to monitor!

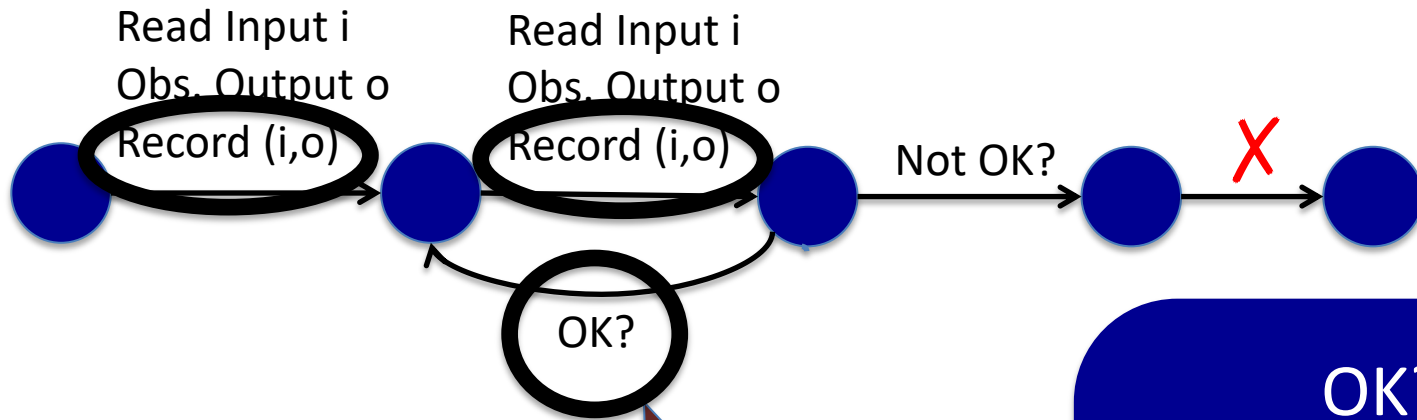
# Monitoring Data Minimization (Program-in-loop)

Reduction to a *trace property*

Not very important (algorithm is simpler)



# Monitor for Data Minimization



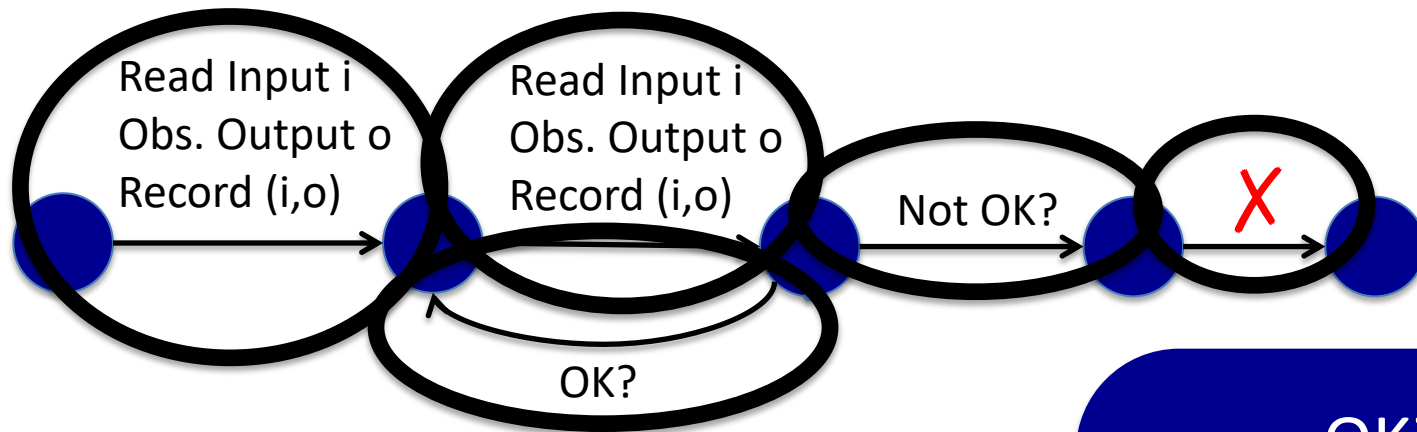
The "intelligence" is in the OK? predicate

OK?  
(Monolithic Data Minimization)

Is there a prefix with the same output and different input?

Input	Output
$i_1$	$o_1$
$i_2$	$o_2$
$i_3$	$o_3$
...	...

# Monitor for *Monolithic* Data Minimization



Input	Output
1200	F
5000	T
90000	T

OK?  
(Monolithic  
Data Minimization)

Is there a prefix  
with the same  
output and  
different input?

# Monitor for *Strong Distributed* Data Minimization

- Monitor very similar to monolithic case but reading inputs from all sources independently
  - More states to read from all sources
- The **OK?** predicate will be different
- (A bit more complex – more theoretical results in Tech Rep *Monitoring Data Minimisation*)

Is that All?



# Other (hyper)properties *similar* to Data Minimization

- *Non-interference*
- *Integrity*
- Software doping (or rather *doping-free programs*)

# Non-interference

- $P$  satisfies **non-interference** if every pair of traces with the same (initial) *low* observation remains indistinguishable for low users
- Absence of strong dependency between input *secret (high)* and output *public (low)*
  - The (public) output observed by the low security users should only depend on low input information

$$\forall \pi, \forall \pi' : (\pi_{I,L} = \pi'_{I,L}) \implies (\pi_{O,L} = \pi'_{O,L})$$

# Integrity

- **Integrity** requires that *high* behaviour of a system should not be influenced by *low* inputs (that can be potentially altered by a malicious user)
- Traces having the same high inputs but possibly different low inputs should have the same high outputs

$$\forall \pi, \forall \pi' : (\pi_{I,H} = \pi'_{I,H}) \implies (\pi_{O,H} = \pi'_{O,H})$$

# Doping-Free Programs

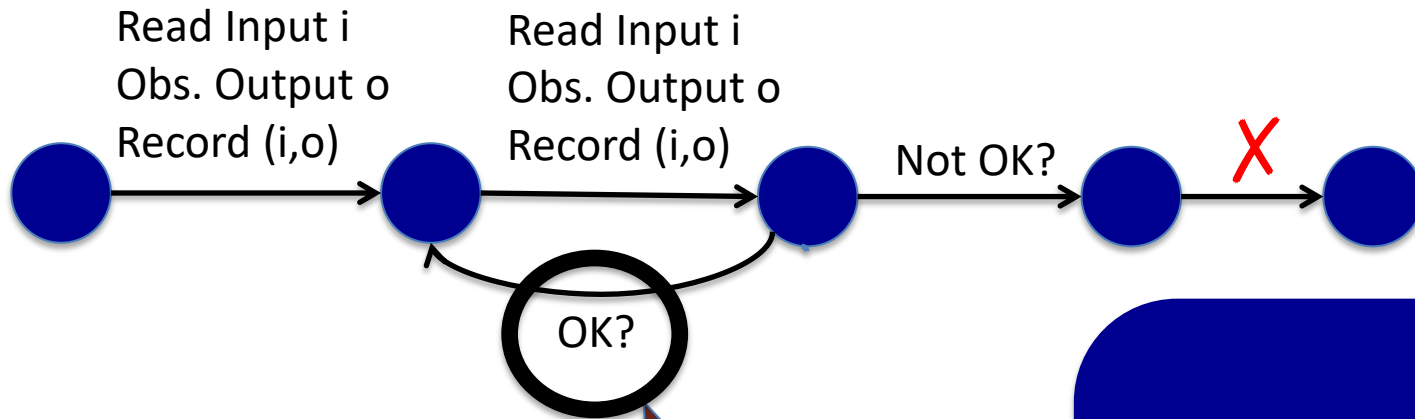
- $P$  is **doping-free** if small variations in the input produces small variations in the output
- A *parameterized* program  $P$  is doping-free if for all pairs of parameters of interest  $p$  and  $p'$ , and input  $i$ , then  $P_p(i) = P_{p'}(i)$

$$\forall \pi, \forall \pi' : ((\pi_{Param} \in PIntrs) \wedge (\pi'_{Param} \in PIntrs) \wedge (\pi_I = \pi'_I)) \\ \implies (\pi_O = \pi'_O))$$

# Other (hyper)properties *similar* to Data Minimization

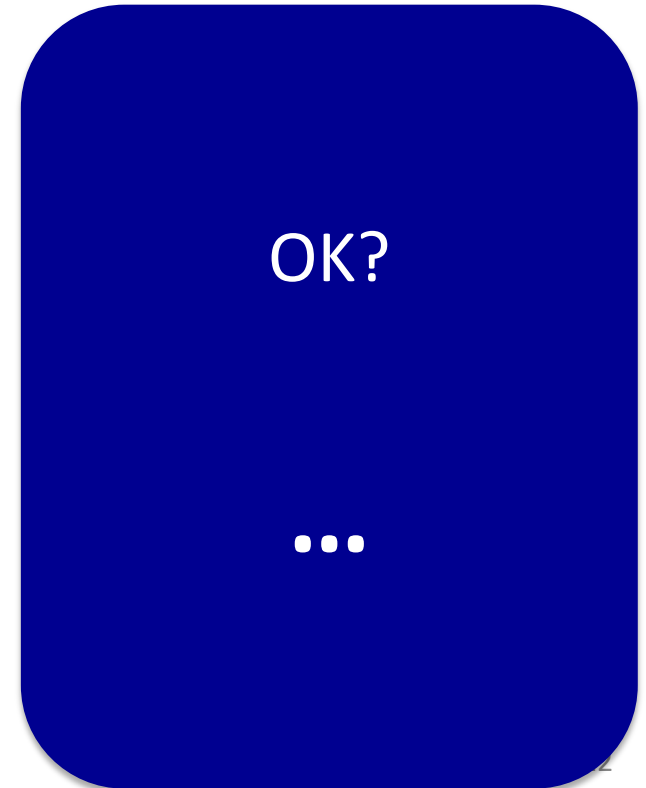
Property	Property expressed in Hyper <sub>2S</sub>
Data minimisation (Monolithic minimality)	$\forall \pi, \forall \pi' : \pi_I \neq \pi'_I \implies \pi_O \neq \pi'_O.$
Non-Interference	$\forall \pi, \forall \pi' : (\pi_{I,L} = \pi'_{I,L}) \implies (\pi_{O,L} = \pi'_{O,L})$
Integrity	$\forall \pi, \forall \pi' : (\pi_{I,H} = \pi'_{I,H}) \implies (\pi_{O,H} = \pi'_{O,H})$
Software doping (doping free program)	$\forall \pi, \forall \pi' :$ $((\pi_{Param} \in PIntrs) \wedge (\pi'_{Param} \in PIntrs) \wedge (\pi_I = \pi'_I))$ $\implies (\pi_O = \pi'_O)$
Strong distributed minimality	$\forall \pi, \forall \pi',$ $\text{let } \pi_I = (i_1, \dots, i_n), \pi'_I = (i'_1, \dots, i'_n).$ $(\exists x \in [1, n] : i_x \neq i'_x \wedge$ $\forall y \in [1, n] : y \neq x \implies i_y = i'_y) \implies \pi_O \neq \pi'_O.$

# Monitor for other Hyperproperties in HyperLTL<sub>2S</sub>



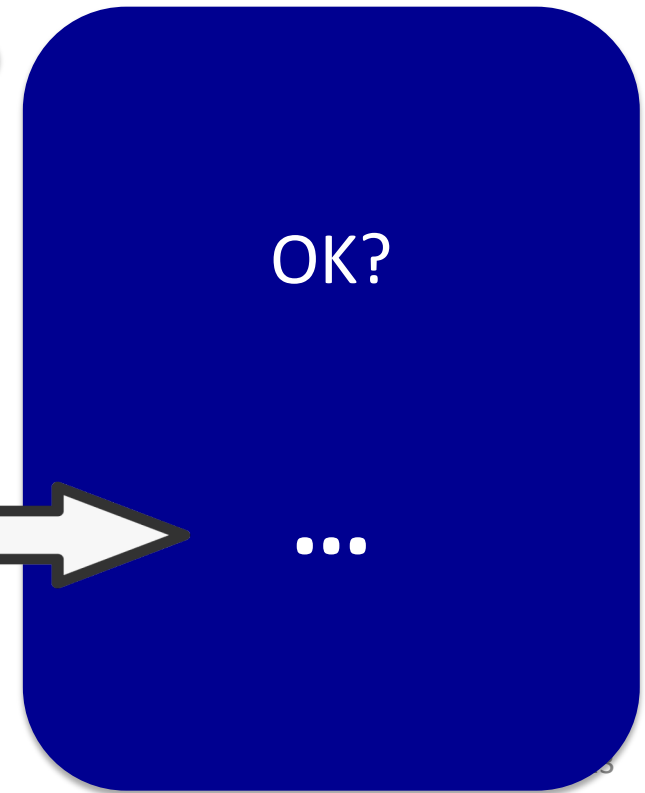
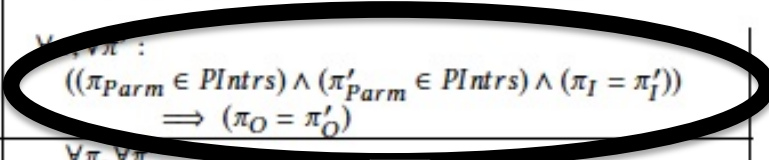
Input	Output
$i_1$	$o_1$
$i_2$	$o_2$
$i_3$	$o_3$
...	...

The “intelligence” is in the **OK?** predicate



# Parameterized Monitor for Hyperproperties in HyperLTL<sub>2S</sub>

Property	Property expressed in Hyper <sub>2S</sub>
Data minimisation (Monolithic minimality)	$\forall \pi, \forall \pi' : \pi_I \neq \pi'_I \Rightarrow \pi_O \neq \pi'_O.$
Non-Interference	$\forall \pi, \forall \pi' : (\pi_{I,L} = \pi'_{I,L}) \Rightarrow (\pi_{O,L} = \pi'_{O,L})$
Integrity	$\forall \pi, \forall \pi' : (\pi_{I,H} = \pi'_{I,H}) \Rightarrow (\pi_{O,H} = \pi'_{O,H})$
Software doping (doping free program)	$\forall \pi, \forall \pi' : ((\pi_{Param} \in PIntrs) \wedge (\pi'_{Param} \in PIntrs) \wedge (\pi_I = \pi'_I)) \Rightarrow (\pi_O = \pi'_O)$
Strong distributed minimality	$\forall \pi, \forall \pi' ,$ let $\pi_I = (i_1, \dots, i_n), \pi'_I = (i'_1, \dots, i'_n).$ $(\exists x \in [1, n] : i_x \neq i'_x$ $\forall y \in [1, n] : y \neq x \Rightarrow i_y = i'_y) \Rightarrow \pi_O \neq \pi'_O.$



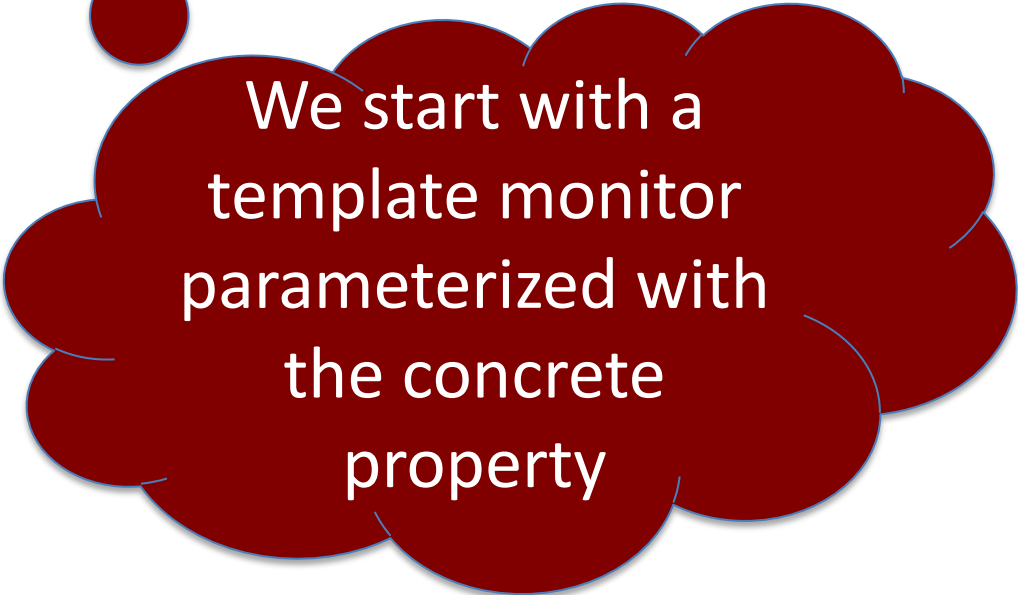
# Runtime Verification (Monitoring) but...

(an unimportant clarifying note)

- The RV technique we are using here doesn't follow the "standard" way of getting the monitor



We don't extract the monitor *from* the property

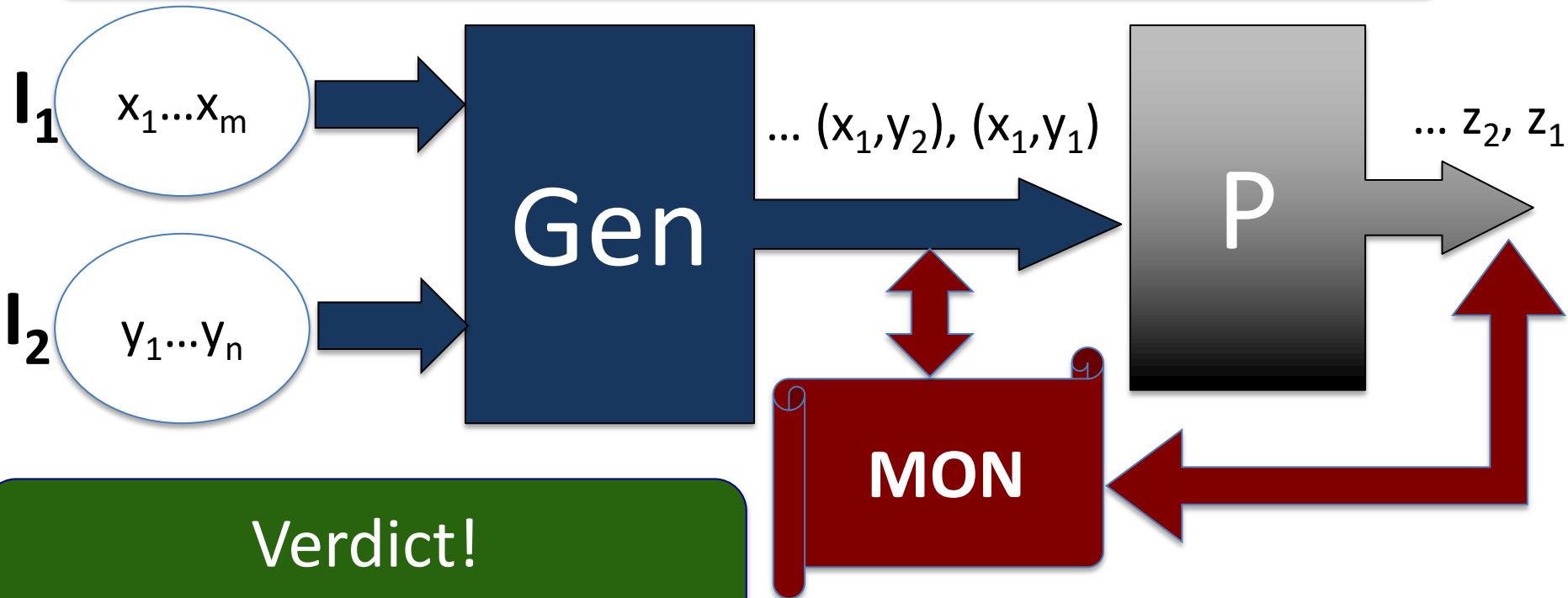


We start with a template monitor parameterized with the concrete property



# (Controlled) Offline Monitoring Data Minimization

Assumption: Finite input domain



Generate the minimizer!  
(Black box)

# Summary

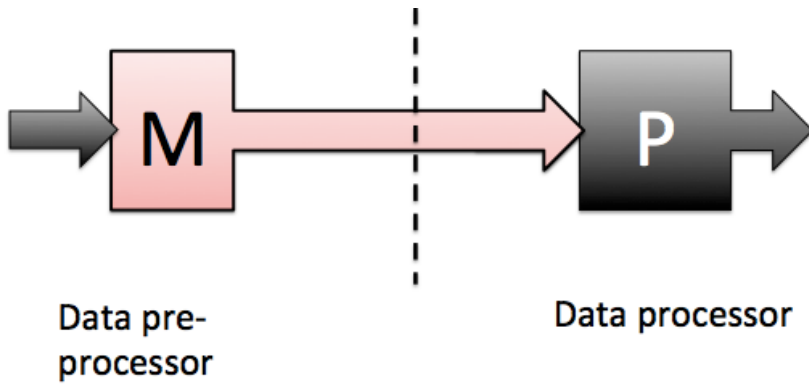
- **Parameterized monitor** for **HyperLTL<sub>2s</sub>**
- Online monitorability for violations of property
  - Generalizes to traces of fixed length (not only 1)
  - Order of the traces not important (they may be reordered)
- Complexity: quadratic in the length of the observed trace
- Offline monitoring under assumption of finite input domains
  - Decidable (trivial!)
  - For data minimization: extraction of a **minimizer**
  - Optimizations are possible (taking into account size of output domain, etc)

# Questions?

M is a *monolithic pre-processor* for P iff

$$P \circ M = P$$

$$M \circ M = M$$



Distributed Minimiser

